

# KATWA COLLEGE

B.Sc 5th Sem Internal Assessment Examination-2019

Subject : Physics

Paper : CC-XI(H)

Time :30 minutes

FM-10

Answer any five question:

- a) Find the commutator  $[\hat{A}, \hat{B}]$  where  $\hat{A} = x^3$  and  $\hat{B} = x \frac{d}{dx}$ .
- b) The operator  $(x + \frac{d}{dx})$  has the eigen value  $\alpha$ . Derive the corresponding eigenfunction.
- c) i> A wave function  $\Psi(\vec{r}, t)$  is admissible if
  - (p)  $\Psi$  is single-valued and finite
  - (q)  $\Psi$  is finite
  - (r)  $\Psi$  is single-valued
  - (s)  $\Psi$  is finite and multivalued
- ii> Which of the wave function is the solution of Schrödinger equation
  - (p)  $A \sec(x)$
  - (q)  $A \exp(-x^2)$
  - (r)  $A \tan(x)$
  - (s)  $A \exp(x^2)$
- d) A plane wave is given by the wave function  $\Psi(x) = Ae^{ikx}$  in one-dimension. Find the probability current density.
- e) If  $\Psi_1(x, t)$  and  $\Psi_2(x, t)$  are both the solutions of Schrödinger's wave equation for a given potential  $V(x, t)$ , then show that  $\Psi = a_1 \Psi_1 + a_2 \Psi_2$  in which  $a_1$  and  $a_2$  are arbitrary constants is also a solution.
- f) The wavefunction of a particle constrained to move along  $x$  ( $-\infty < x < +\infty$ ) at a certain instant is given by  $\Psi(x) = Ae^{-\frac{x^2}{a^2} + ibx}$  [ $a, b$  are real constants]. Find the normalization constant  $A$ .
- g) Find the expectation value of the momentum of a particle free to move in a one-dimensional space of zero potential from  $x = -\infty$  to  $+\infty$ .

